

**Research paper****Short Note: Delayed Neuromorphic Systems***Yousef Azizi¹, Majid Mohseni^{1,2*}* ¹*Department of Physics, Shahid Beheshti University, Tehran, Iran*²*NBIC Center, Shahid Beheshti University, Tehran, Iran***m-mohseni@sbu.ac.ir***Article info:****Article history:**

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Abstract

Delayed neuromorphic systems mimic biological neural networks by incorporating time delays, enabling complex dynamics like oscillations and high-dimensional behaviour for tasks. Time-delay reservoir computing, using minimal hardware, achieves efficient, low-power processing at high speeds. Challenges include architectural trade-offs, limited delay tunability, simulation complexity, and stability control. This note examines the potential and limitations of these systems for scalable, energy-efficient computing in edge devices and brain-machine interfaces.

Introducing time delays into dynamical systems can significantly enrich their behaviour, giving rise to phenomena such as limit cycles, sustained oscillations, metastability, and even chaotic dynamics [1,3]. In neuroscience, synaptic and axonal transmission delays are inherent due to the finite propagation speed of action potentials and the biochemical processes involved in neurotransmission. These delays are not merely passive lags but actively shape network dynamics, influencing synchronization, information processing, and emergent computational properties—even in small neural, electrical and spin circuits [3-7]. Neuromorphic engineering aims to emulate the structure and function of biological neural systems, including spiking dynamics, memory, learning, and energy-efficient computation. Given the ubiquity of delays in real neural systems, incorporating them into neuromorphic designs is

both biologically plausible and functionally advantageous. Delayed coupling has been explored in various neuromorphic architectures—not only as a realistic feature but also as a mechanism to enhance computational capabilities, stabilize network states, or enable temporal processing. Common approaches to implement delays include external feedback circuits, optoelectronic delay lines, transmission lines, and intrinsic device-level dynamics (e.g., memristive relaxation) [8].

Notably, Appeltant et al. (2011) demonstrated that a single nonlinear node with delayed feedback can emulate a large-scale recurrent neural network, forming the basis of time-delay reservoir computing (RC)—a paradigm that has since been realized in photonic, electronic, and mechanical systems [1]. This concept has been further advanced by Fischer, Larger, and colleagues, who have pioneered high-speed



photonic implementations of delay-based neuromorphic systems capable of processing gigabit-per-second data streams [9-14].

Despite these promising developments, several fundamental challenges remain in the design and deployment of delayed neuromorphic systems. This note briefly addresses the benefits and limitations of introducing delays in such systems, highlighting current research directions and open problems.

The inclusion of time delays endows neuromorphic systems with enhanced computational expressiveness. Delays allow the system to implicitly maintain a history of past inputs, enabling rich temporal integration and nonlinear mixing of signals over time. This property is particularly valuable for tasks involving time-series prediction, speech processing, and reservoir computing, where temporal correlations are essential [15].

Moreover, delayed systems can exhibit high-dimensional dynamics even with minimal hardware—such as a single neuron with delayed feedback—effectively enabling compact neuromorphic platforms to process arbitrarily long input sequences. This concept underpins delay-coupled reservoir computing, which drastically reduces the need for large-scale networks and lowers power consumption [1]. For instance, photonic delay systems developed by Larger, Brunner, and Fischer have demonstrated real-time processing of spoken digits and channel equalization at speeds exceeding 1 Gb/s [9-12].

However, despite these advantages, several challenges persist:

Architectural Trade-offs: Introducing delays via external circuits (e.g., analog delay lines or digital buffers) may compromise the compactness, speed, and energy efficiency that are central to neuromorphic design principles. Such solutions can also introduce noise and latency bottlenecks [16].

Limited Flexibility: The functional form and tunability of delays depend heavily on implementation (electronic, photonic, memristive, etc.). Many current designs offer fixed or narrowly adjustable delay times, limiting adaptability across tasks [11].

Simulation Complexity: Modeling delayed neuromorphic systems typically involves solving delay differential equations (DDEs), which are computationally expensive even for small networks. For systems with multiple incommensurate delays (i.e., delays with irrational ratios), numerical integration becomes increasingly challenging, and efficient simulation frameworks are still under development [14].

Stability and Control: Delays can destabilize feedback loops, leading to unwanted oscillations or chaotic behavior. Ensuring stable operation while preserving useful dynamics remains a key challenge in both design and control [13].

Incorporating time delays into neuromorphic systems holds significant promise for enhancing computational capacity, enabling efficient temporal processing, and achieving brain-inspired dynamics with minimal hardware. As demonstrated by Appeltant, Fischer, and collaborators, even a single nonlinear unit with delayed feedback can perform complex tasks such as speech recognition and time-series prediction, forming the foundation of scalable, low-power neuromorphic platforms [1,9].

While delays introduce practical challenges related to implementation, simulation, and stability, they also open new opportunities for compact, adaptive, and biologically realistic computing paradigms. With growing interest in edge computing, low-power AI, and brain-machine interfaces, delayed neuromorphic systems represent a rapidly evolving frontier. Continued advances in materials, circuit design, and numerical methods will likely overcome current limitations, positioning delay-based neuromorphic computing as a pivotal technology in next-generation intelligent systems.

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